## Outline

- Buffer Solutions
- Titrations
- Solubility Equilibria
- Precipitation Problems
- Lewis Acids and Bases
- Complex Ion Equilibria
- Solubility - An Equilibrium Position


## Buffers

Buffers are solutions that resist changes in pH
Buffers contain significant amounts of a weak acid (HA) and its conjugate base ( $\mathrm{A}^{-}$)

HA neutralizes added base:

$$
\mathrm{HA}+\mathrm{OH}^{-} \rightarrow \mathrm{A}^{-}+\mathrm{H}_{2} \mathrm{O}
$$

$A^{-}$neutralizes added acid:

$$
\mathrm{A}^{-}+\mathrm{H}_{3} \mathrm{O}^{+} \rightarrow \mathrm{HA}+\mathrm{H}_{2} \mathrm{O}
$$

Resistance to pH change increases with increasing concentrations of the weak acid and its conjugate base

Acids ionize to form the conjugate base...

|  | $\mathrm{HA}(\mathrm{aq}) \rightleftharpoons$ | $\mathrm{H}^{+}(\mathrm{aq})+\mathrm{A}^{-}(\mathrm{aq})$ |  |
| :---: | :---: | :---: | :---: |
| I | $[\mathrm{HA}]$ | 0 | $\left[\mathrm{~A}^{-}\right]$ |
| E | $[\mathrm{HA}]-\mathrm{x}$ | x | $\left[\mathrm{A}^{-}\right]+\mathrm{x}$ |

$\mathrm{K}_{\mathrm{a}}=\frac{\left[\mathrm{H}^{+}\right]_{\mathrm{eq}}\left(\left[\mathrm{A}^{-}\right]+\mathrm{x}\right)}{([\mathrm{HA}]-\mathrm{x})} \approx \frac{\left[\mathrm{H}^{+}\right]_{\mathrm{eq}}\left(\left[\mathrm{A}^{-}\right]\right)}{([\mathrm{HA}])}$
$\Rightarrow \quad-\log \left(\mathrm{K}_{\mathrm{a}}\right)=-\log \left(\frac{\left[\mathrm{H}^{+}\right]_{\mathrm{eq}}\left(\left[\mathrm{A}^{-}\right]\right)}{([\mathrm{HA}])}\right)$
$\Rightarrow \mathrm{pH}=\mathrm{pK}_{\mathrm{a}}+\log \left(\frac{\left[\mathrm{A}^{-}\right]}{[\mathrm{HA}]}\right) \quad$ Henderson-Hasselbalch Eq.

The pH of a buffer is determined by the ratio of $\left[\mathrm{A}^{-}\right.$] to [HA]
Solutions resist pH changes when...

$$
0.1<\frac{\left[\mathrm{A}^{-}\right]}{[\mathrm{HA}]}<10
$$

A buffer is most effective when the $\left[A^{-}\right]=[H A] \ldots$

$$
\mathrm{pH}=\mathrm{pK}_{\mathrm{a}}+\log \left(\frac{\left[\mathrm{A}^{-}\right]}{[\mathrm{HA}]}\right) \Rightarrow \mathrm{pH}=\mathrm{pK}_{\mathrm{a}}+\log (1) \Rightarrow \mathrm{pH}=\mathrm{pK}_{\mathrm{a}}
$$

To make an effective buffer at a specific pH ... choose weak acid with $\mathrm{pK}_{\mathrm{a}}+/-1$ to the desired pH

A buffer is made by mixing...

1. a weak acid and a salt of its conjugate base
2. a weak base and a salt of its conjugate acid
3. a weak acid and a lesser amount of a strong base
4. a weak base and a lesser amount of a strong acid

You want a $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H} / \mathrm{CH}_{3} \mathrm{CO}_{2}^{-}$buffer with a pH of $5.00\left(\mathrm{~K}_{\mathrm{a}}=1.8\right.$ $\left.\times 10^{-5}\right)$. Find the $\left[\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right] /\left[\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}\right]$ratio in this buffer.
$\mathrm{pK}_{\mathrm{a}}=-\log \left(\mathrm{K}_{\mathrm{a}}\right)=-\log \left(1.8 \times 10^{-5}\right)=4.74$
$\mathrm{pH}=\mathrm{pK}_{\mathrm{a}}+\log \left(\frac{\left[\mathrm{A}^{-}\right]}{[\mathrm{HA}]}\right) \Rightarrow \quad 5.00=4.74+\log \left(\frac{\left[\mathrm{A}^{-}\right]}{[\mathrm{HA}]}\right)$
$\log \left(\frac{\left[\mathrm{A}^{-}\right]}{[\mathrm{HA}]}\right)=0.26 \Rightarrow \frac{\left[\mathrm{~A}^{-}\right]}{[\mathrm{HA}]}=1.82 \Rightarrow \frac{[\mathrm{HA}]}{\left[\mathrm{A}^{-}\right]}=\underline{0.55}$

What must be the molarity of sodium fluoride in a solution of 0.10 M hydrofluoric acid ( $\mathrm{K}_{\mathrm{a}}=3.5 \times 10^{-4}$ ) to make a buffer with a pH of 4.00 ?

$$
\begin{aligned}
& \mathrm{pH}=\mathrm{pK}_{\mathrm{a}}+\log \left(\frac{\left[\mathrm{A}^{-}\right]}{[\mathrm{HA}]}\right) \Rightarrow 4.00=3.46+\log \left(\frac{\left[\mathrm{A}^{-}\right]}{0.10 \mathrm{M}}\right) \\
& \log \left(\frac{\left[\mathrm{A}^{-}\right]}{0.10 \mathrm{M}}\right)=0.54 \Rightarrow \frac{\left[\mathrm{~A}^{-}\right]}{0.10 \mathrm{M}}=3.46 \Rightarrow\left[\mathrm{~A}^{-}\right]=\underline{0.35 \mathrm{M}}
\end{aligned}
$$

Find the pH of 1.00 L of buffer solution that is 1.00 M in acetic acid $\left(K_{a}=1.76 \times 10^{-5}\right)$ and 1.00 M sodium acetate if 0.01 moles of NaOH are added.

$$
\frac{0.01 \mathrm{~mol} \mathrm{NaOH}}{1.00 \mathrm{~L}}=0.01 \mathrm{M} \mathrm{NaOH} \Rightarrow \underline{0.01 \mathrm{M} \mathrm{OH}^{-}}
$$

$$
\mathrm{OH}^{-}(\mathrm{aq})+\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(\mathrm{aq}) \rightarrow \mathrm{H}_{2} \mathrm{O}(\mathrm{I})+\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(\mathrm{aq})
$$

| I | 0.01 | 1.00 | 1.00 |
| :---: | :---: | :---: | :---: |
| F | 0 | 0.99 | 1.01 |

$$
\mathrm{pH}=\mathrm{pK}_{\mathrm{a}}+\log \left(\frac{\left[\mathrm{A}^{-}\right]}{[\mathrm{HA}]}\right)=-\log \left(1.76 \times 10^{-5}\right)+\log \left(\frac{1.01}{0.99}\right)=\underline{4.76}
$$

Find the pH of 1.00 L of buffer solution that is 1.00 M in acetic acid $\left(K_{a}=1.76 \times 10^{-5}\right)$ and 1.00 M sodium acetate if 0.01 moles of HCl are added.
$\frac{0.01 \mathrm{~mol} \mathrm{HCl}}{1.00 \mathrm{~L}}=0.01 \mathrm{M} \mathrm{HCl} \Rightarrow 0.01 \mathrm{M} \mathrm{H}^{+}$

|  | $\left.\mathrm{H}^{+}(\mathrm{aq})+\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}-\mathrm{aq}\right)$ |  | $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(\mathrm{aq})$ |  |
| :---: | :---: | :---: | :---: | :---: |
| I | 0.01 | 1.00 | 1.00 |  |
| F | 0 | 0.99 | 1.01 |  |
| $\mathrm{pH}=\mathrm{pK}_{\mathrm{a}}+\mathrm{log}$ |  | ) $)=-\log \left(1.76 \times 10^{-5}\right)+\log \left(\frac{0.99}{1.01}\right)=\underline{4.75}$ |  |  |

## Titrations

Three types of titrations to consider...

1. strong acid and strong base: $\mathrm{H}^{+}+\mathrm{OH}^{-} \rightarrow \mathrm{H}_{2} \mathrm{O}$
2. strong acid and weak base:

$$
\begin{aligned}
& \mathrm{H}^{+}+\mathrm{B} \rightarrow \mathrm{HB}^{+} \\
& \mathrm{HB}^{+} \rightleftharpoons \mathrm{B}+\mathrm{H}^{+}
\end{aligned}
$$

3. weak acid and strong base:

$$
\begin{aligned}
& \mathrm{HA}+\mathrm{OH}^{-} \rightarrow \mathrm{A}^{-}+\mathrm{H}_{2} \mathrm{O} \\
& \mathrm{~A}^{-}+\mathrm{H}_{2} \mathrm{O} \rightleftharpoons \mathrm{HA}+\mathrm{OH}^{-}
\end{aligned}
$$

## Strong - Strong Titrations

250.0 mL of 0.020 M NaOH is titrated with 0.10 M HCl . Calculate the pH of the solution after the addition of...
a. 10.0 mL HCl

Find molarities... $\left[\mathrm{OH}^{-}\right]=0.019 \mathrm{M}$ and $\left[\mathrm{H}^{+}\right]=0.0038 \mathrm{M}$

\[

\]

b. 50.0 mL HCl

Find molarities... $\quad\left[\mathrm{OH}^{-}\right]=0.017 \mathrm{M}$ and $\left[\mathrm{H}^{+}\right]=0.017 \mathrm{M}$

|  | $\mathrm{H}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})$ | $\rightarrow$ | $\mathrm{H}_{2} \mathrm{O}(\mathrm{I})$ |  |
| :---: | :---: | :---: | :---: | :---: |
| I | 0.017 | 0.017 |  |  |
| F | 0 | 0 |  |  |

amount acid = amount base... stoichiometric point!
strong acid - strong base titrations: $\mathrm{pH}=7.00$ at stoichiometric point

## c. 100.0 mL HCl

Find molarities... $\quad\left[\mathrm{OH}^{-}\right]=0.014 \mathrm{M}$ and $\left[\mathrm{H}^{+}\right]=0.029 \mathrm{M}$

\[

\]

Titration curve is plot of pH vs. acid (base) added



## Strong - Weak Titrations

Strong acid (base) - weak base (acid) titration curves have four regions:
(a) initial, (b) buffer, (c) stoichiometric point, (d) excess


100.0 mL of 0.10 M acetic acid $\left(\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right), \mathrm{K}_{\mathrm{a}}=1.76 \times 10^{-5}$, is titrated with 1.0 M sodium hydroxide. Determine the pH of the solution with...
a. 0 mL NaOH added (initial)

|  | $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(\mathrm{aq})$ | $\rightleftharpoons$ | $\mathrm{H}^{+}(\mathrm{aq})+\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(\mathrm{aq})$ |
| :---: | :---: | :---: | :---: |
| I | 0.10 | 0 | 0 |
| E | $0.10-\mathrm{x}$ | x | x |

$$
\begin{aligned}
& 1.76 \times 10^{-5}=\frac{\mathrm{x}^{2}}{(0.10-\mathrm{x})} \approx \frac{\mathrm{x}^{2}}{(0.10)} \Rightarrow \mathrm{x}=1.3 \times 10^{-3} \mathrm{M}=\left[\mathrm{H}^{+}\right] \\
& \mathrm{pH}=-\log \left(1.3 \times 10^{-3} \mathrm{M}\right)=2.89
\end{aligned}
$$

## b. 2.5 mL NaOH added (buffer)

Find molarities:
$\left[\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right]=0.098 \mathrm{M}$ and $\left[\mathrm{OH}^{-}\right]=0.024 \mathrm{M}$

| $\mathrm{OH}^{-}(\mathrm{aq})+\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(\mathrm{aq})$ |  |  |  |
| :---: | :---: | :---: | :---: |
| I | 0.024 | 0.098 | $\mathrm{H}_{2} \mathrm{O}(\mathrm{I})+\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(\mathrm{aq})$ |
| F | 0 | 0.074 | 0 |
|  |  | 0.024 |  |
| $\mathrm{pH}=$ | $\mathrm{pK}_{\mathrm{a}}+\log \left(\frac{\left[\mathrm{A}^{-}\right]}{[\mathrm{HA}]}\right)=-\log \left(1.76 \times 10^{-5}\right)+\log \left(\frac{0.024}{0.074}\right)=4.27$ |  |  |

## c. 10.0 mL NaOH added (stoichiometric point)

Find molarities:

$$
\left[\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right]=0.091 \mathrm{M} \text { and }\left[\mathrm{OH}^{-}\right]=0.091 \mathrm{M}
$$

|  | $\mathrm{OH}^{-}(\mathrm{aq})+\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(\mathrm{aq})$ | $\rightarrow$ | $\mathrm{H}_{2} \mathrm{O}(\mathrm{I})+\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(\mathrm{aq})$ |
| :---: | :---: | :---: | :---: | :---: |
| I | 0.091 | 0.091 | 0 |
| F | 0 | 0 | 0.091 |

Not a buffer... Consider the ionization of the conjugate base!
c. 10.0 mL NaOH added (stoichiometric point)

$$
\begin{aligned}
& \mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O} \rightleftharpoons \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq}) \\
& \begin{array}{llll}
\mathrm{I} & 0.091 & 0 & 0
\end{array} \\
& \text { E } 0.091-x \quad x \quad x \\
& \mathrm{~K}_{\mathrm{b}}=\frac{\mathrm{K}_{\mathrm{w}}}{\mathrm{~K}_{\mathrm{a}}}=\frac{1.0 \times 10^{-14}}{1.76 \times 10^{-5}}=5.68 \times 10^{-10} \\
& 5.68 \times 10^{-10}=\frac{x^{2}}{(0.091-x)} \approx \frac{x^{2}}{(0.091)} \Rightarrow x=7.2 \times 10^{-6} M=\left[\mathrm{OH}^{-}\right] \\
& \mathrm{pOH}=-\log \left(7.2 \times 10^{-6} \mathrm{M}\right)=5.14 \Rightarrow \mathrm{pH}=14.00-5.14=8.86
\end{aligned}
$$

## d. 12.5 mL NaOH added (excess)

Find molarities:

$$
\left[\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right]=0.089 \mathrm{M} \text { and }\left[\mathrm{OH}^{-}\right]=0.11 \mathrm{M}
$$

|  | $\mathrm{OH}^{-}(\mathrm{aq})+\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(\mathrm{aq})$ | $\rightarrow$ | $\mathrm{H}_{2} \mathrm{O}(\mathrm{I})+\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(\mathrm{aq})$ |
| :---: | :---: | :---: | :---: |
| I | 0.11 | 0.089 | 0 |
| F | 0.02 | 0 | 0.089 |

$\mathrm{pOH}=-\log (0.02 \mathrm{M})=1.7$
$\mathrm{pH}=14.00-1.7=\underline{12.3}$

Stoichiometric point can be identified with...

1. pH meter: monitor pH during titration stoichiometric point is middle of steep change
2. indicator: weak acid (c. base) changes during titration

$$
\mathrm{HIn} \underset{\mathrm{H}^{+}}{\stackrel{\mathrm{OH}^{-}}{\rightleftharpoons}} \mathrm{In}^{-}
$$

end point indicated by color change
want $\mathrm{pK}_{\mathrm{a}}=\mathrm{pH}+/-1$ at stoichiometric point

A weakly acidic solution is prepared by dissolving 1.016 g benzoic acid into 25.00 mL water, and titrated with 0.2040 M NaOH .
$\mathrm{MM}=122.12 \mathrm{~g} / \mathrm{mol}$ and $\mathrm{K}_{\mathrm{a}}=6.4 \times 10^{-5}$
a. How many mL's to reach stoichiometric point?
$1.016 \mathrm{~g} \mathrm{BH} \times \frac{1 \mathrm{~mol} \mathrm{BH}}{122.12 \mathrm{gBH}} \times \frac{1}{0.02500 \mathrm{~L}}=0.3328 \mathrm{M}$
$25.00 \mathrm{~mL} \times \frac{0.3328 \mathrm{~mol}}{1 \mathrm{~L}} \times \frac{1 \mathrm{~mol} \mathrm{NaOH}}{1 \mathrm{~mol} \mathrm{BH}} \times \frac{1 \mathrm{~L}}{0.2040 \mathrm{~mol}}=40.78 \mathrm{~mL}$
b. What is pH at stoichiometric point?

Find molarities:

$$
[\mathrm{BH}]=0.1265 \mathrm{M} \text { and }\left[\mathrm{OH}^{-}\right]=0.1265 \mathrm{M}
$$

$$
\begin{array}{ccccc} 
& \mathrm{OH}^{-}(\mathrm{aq})+\mathrm{BH}(\mathrm{aq}) & \rightarrow & \mathrm{H}_{2} \mathrm{O}(\mathrm{I})+\mathrm{B}^{-}(\mathrm{aq}) \\
\mathrm{I} & 0.1265 & 0.1265 & 0 \\
\mathrm{~F} & 0 & 0 & 0.1265
\end{array}
$$

b. What is pH at stoichiometric point?

$$
\begin{aligned}
& \mathrm{B}^{-}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O} \rightleftharpoons \mathrm{BH}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq}) \\
& \text { I } 0.1265 \\
& \text { E 0.1265-x } \\
& 0 \quad 0 \\
& \text { x } \quad \mathrm{x} \\
& \mathrm{~K}_{\mathrm{b}}=\frac{\mathrm{K}_{\mathrm{w}}}{\mathrm{~K}_{\mathrm{a}}}=\frac{1.0 \times 10^{-14}}{6.4 \times 10^{-5}}=1.56 \times 10^{-10} \\
& 1.56 \times 10^{-10}=\frac{x^{2}}{(0.1265-x)} \approx \frac{x^{2}}{(0.1265)} \\
& \mathrm{x}=4.5 \times 10^{-6} \mathrm{M}=\left[\mathrm{OH}^{-}\right] \quad(0.004 \%) \\
& \mathrm{pOH}=-\log \left(4.44 \times 10^{-6} \mathrm{M}\right)=5.35 \Rightarrow \mathrm{pH}=\underline{8.65}
\end{aligned}
$$

c. What indicator should be used? What color change occurs?
$8.65+/-1=7.65$ and 9.65
thymol blue (chose closest!)
yellow (acidic) $\rightarrow$ blue (basic)

| Indicator | $\mathrm{pK}_{\mathrm{a}}$ | Acidic Color | Basic Color |
| :--- | :--- | :--- | :--- |
| methyl red | 5.0 | red | yellow |
| phenol red | 7.9 | yellow | red |
| thymol blue | 8.9 | yellow | blue |
| phenolphthalein | 9.4 | colorless | pink |

## Solubility Equilibria

Solids dissolve (dissociate) and ions precipitate (associate) in a competing process

Equilibrium achieved when rate of dissolution and precipitation are equal

$$
\mathrm{AB}(\mathrm{~s}) \rightleftharpoons \mathrm{A}^{+}(\mathrm{aq})+\mathrm{B}^{-}(\mathrm{aq}) \quad \mathrm{K}_{\mathrm{eq}}=\left[\mathrm{A}^{+}\right]\left[\mathrm{B}^{-}\right]
$$

A $\mathrm{K}_{\text {eq }}$ for a salt dissociating in water is called a $\mathrm{K}_{\text {sp }}$, the solubility product constant

Solubility is the amount of substance that can be dissolved

The solubility of calcium fluoride is $0.017 \mathrm{~g} / \mathrm{L}$. Find its $\mathrm{K}_{\mathrm{sp}}$.

$$
\begin{array}{ccc}
\mathrm{CaF}_{2}(\mathrm{~s}) & \rightleftharpoons & \mathrm{Ca}^{2+}(\mathrm{aq}) \\
\mathrm{I} & 0 & 2 \mathrm{~F}^{-}(\mathrm{aq}) \\
\mathrm{E} & & 0 \\
& \mathrm{x} & 2 \mathrm{x}
\end{array}
$$

$x=$ solubility of $\mathrm{CaF}_{2}$ in $\mathrm{mol} / \mathrm{L}$

$$
\begin{aligned}
& \mathrm{x}=\frac{0.017 \mathrm{~g} \mathrm{CaF}_{2}}{\mathrm{~L}} \times \frac{1 \mathrm{~mol} \mathrm{CaF}_{2}}{78.1 \mathrm{~g} \mathrm{CaF}_{2}}=2.2 \times 10^{-4} \mathrm{M} \\
& \mathrm{~K}_{\mathrm{sp}}=\left[\mathrm{Ca}^{2+}\right]\left[\mathrm{F}^{-}\right]^{2}=(\mathrm{x})(2 \mathrm{x})^{2}=4 \mathrm{x}^{3}=4.3 \times 10^{-11}
\end{aligned}
$$

The solubility of iron (III) hydroxide (MM = $106.8 \mathrm{~g} / \mathrm{mol}$ ) is 0.130 g for every 100. $\mathrm{mL} . .$. . Find the $\mathrm{K}_{\mathrm{sp}}$.

| $\mathrm{Fe}(\mathrm{OH})_{3}(\mathrm{~s})$ | $\rightleftharpoons$ | $\mathrm{Fe}^{3+}(\mathrm{aq})+3 \mathrm{OH}^{-}(\mathrm{aq})$ |
| :---: | :---: | :---: |
| I | 0 | 0 |
| E |  | x |

$x=$ solubility of $\mathrm{Fe}(\mathrm{OH})_{3}$ in $\mathrm{mol} / \mathrm{L}$
$x=\frac{0.130 \mathrm{~g} \mathrm{Fe}(\mathrm{OH})_{3}}{0.100 \mathrm{~L}} \times \frac{1 \mathrm{~mol} \mathrm{Fe}(\mathrm{OH})_{3}}{106.8 \mathrm{~g} \mathrm{Fe}(\mathrm{OH})_{3}}=1.22 \times 10^{-2} \mathrm{M}$
$\mathrm{K}_{\text {sp }}=\left[\mathrm{Fe}^{3+}\right]\left[\mathrm{OH}^{-}\right]^{3}=(\mathrm{x})(3 \mathrm{x})^{3}=27 \mathrm{x}^{4}=\underline{5.98 \times 10^{-7}}$

Find the molar solubility ( $\mathrm{mol} / \mathrm{L}$ ) of calcium sulfate if its $\mathrm{K}_{\mathrm{sp}}=$ $2.40 \times 10^{-5}$.

| $\mathrm{CaSO}_{4}(\mathrm{~s})$ | $\rightleftharpoons$ | $\mathrm{Ca}^{2+}(\mathrm{aq})$ |
| :---: | :---: | :---: |
| I | 0 | $\mathrm{SO}_{4}^{2-}(\mathrm{aq})$ |
| E | x | 0 |
| I | x |  |

$x=$ molar solubility of $\mathrm{CaSO}_{4}$

$$
\mathrm{K}_{\mathrm{sp}}=\left[\mathrm{Ca}^{2+}\right]\left[\mathrm{SO}_{4}^{2-}\right] \Rightarrow 2.40 \times 10^{-5}=(\mathrm{x})(\mathrm{x}) \Rightarrow \mathrm{x}=\underline{0.00490 \mathrm{M}}
$$

What is the solubility of $\mathrm{CaSO}_{4}(136.2 \mathrm{~g} / \mathrm{mol})$ in $\mathrm{g} / 100 \mathrm{~mL}$ ?

$$
\frac{0.00490 \mathrm{~mol} \mathrm{CaSO}_{4}}{\mathrm{~L}} \times \frac{136.2 \mathrm{~g}}{\mathrm{~mol}} \times \frac{0.1 \mathrm{~L}}{100 \mathrm{~mL}}=\frac{0.0667 \mathrm{~g} \mathrm{CaSO}_{4}}{100 \mathrm{~mL}}
$$

Find the solubility of lead (II) iodide (MW $=461.2 \mathrm{~g} / \mathrm{mol}$ ) in $\mathrm{g} /$ 100 mL if its $\mathrm{K}_{\mathrm{sp}}=8.30 \times 10^{-9}$.

$$
\begin{array}{ccc}
\mathrm{PbI}_{2}(\mathrm{~s}) & \rightleftharpoons & \mathrm{Pb}^{2+}(\mathrm{aq}) \\
\mathrm{I} & 0 & 2 \mathrm{I}^{-}(\mathrm{aq}) \\
\mathrm{E} & \mathrm{x} & 0 \\
& 2 \mathrm{x}
\end{array}
$$

$x=$ molar solubility of $\mathrm{PbI}_{2}$

$$
\mathrm{K}_{\mathrm{sp}}=\left[\mathrm{Pb}^{2+}\right]\left[\mathrm{I}^{-}\right]^{2} \Rightarrow 8.30 \times 10^{-9}=(\mathrm{x})(2 \mathrm{x})^{2} \Rightarrow \mathrm{x}=1.28 \times 10^{-3} \mathrm{M}
$$

$$
\frac{0.00128 \mathrm{~mol} \mathrm{PbI}_{2}}{\mathrm{~L}} \times \frac{461.2 \mathrm{~g}}{\mathrm{~mol}} \times \frac{0.1 \mathrm{~L}}{100 \mathrm{~mL}}=\frac{0.0590 \mathrm{~g} \mathrm{PbI}_{2}}{100 \mathrm{~mL}}
$$

$\mathrm{K}_{\text {sp }}$ 's can be used to compare relative solubilities of salts
Salts with same number of ions: compare $\mathrm{K}_{\mathrm{sp}}$ 's directly!

| Salt | $\mathrm{K}_{\text {sp }}$ | Solubility |
| :--- | :--- | :---: |
| $\mathrm{NiCO}_{3}$ | $1.4 \times 10^{-7}$ | greatest |
| AgOH | $2.0 \times 10^{-8}$ | $\downarrow$ |
| MnS | $2.3 \times 10^{-13}$ | least |

Salts with different number of ions: calculate solubility!

Solubility of a salt is decreased by the presence of ions involved in equilibrium reaction: common ion effect

What is the molar solubility of iron (II) carbonate in 0.10 M sodium carbonate? $\mathrm{K}_{\mathrm{sp}}=2.1 \times 10^{-11}$

$$
\mathrm{Na}_{2} \mathrm{CO}_{3} \Rightarrow 0.20 \mathrm{M} \mathrm{Na}^{+} \text {and } 0.10 \mathrm{M} \mathrm{CO}_{3}{ }^{2-}
$$

$$
\begin{array}{ccc}
\mathrm{FeCO}_{3}(\mathrm{~s}) & \rightleftharpoons & \mathrm{Fe}^{2+}(\mathrm{aq}) \\
\mathrm{I} & 0 & \mathrm{CO}_{3}^{2-}(\mathrm{aq}) \\
\mathrm{E} & \mathrm{x} & 0.10 \\
& \mathrm{x}+0.10
\end{array}
$$

$x=$ molar solubility of $\mathrm{FeCO}_{3}$

$$
\begin{aligned}
& \mathrm{K}_{\mathrm{sp}}=\left[\mathrm{Fe}^{2+}\right]\left[\mathrm{CO}_{3}^{2-}\right] \Rightarrow 2.1 \times 10^{-11}=(x)(x+0.10) \approx(x)(0.10) \\
& x=\underline{2.1 \times 10^{-10} \mathrm{M} \mathrm{FeCO}_{3}}
\end{aligned}
$$

What is the molar solubility of silver phosphate $\left(K_{\text {sp }}=1.8 \times 10^{-18}\right)$ in 0.20 M silver nitrate?
$\mathrm{AgNO}_{3} \Rightarrow 0.20 \mathrm{M} \mathrm{Ag}^{+}$and $0.20 \mathrm{M} \mathrm{NO}_{3}^{-}$

$$
\begin{array}{ccc}
\mathrm{Ag}_{3} \mathrm{PO}_{4}(\mathrm{~s}) & \rightleftharpoons & 3 \mathrm{Ag}^{+}(\mathrm{aq}) \\
\mathrm{I} & 0.20 & \mathrm{PO}_{4}^{3-}(\mathrm{aq}) \\
\mathrm{E} & 3 \mathrm{x}+0.20 & \mathrm{x}
\end{array}
$$

$x=$ molar solubility of $\mathrm{Ag}_{3} \mathrm{PO}_{4}$

$$
\begin{aligned}
& \mathrm{K}_{\mathrm{sp}}=\left[\mathrm{Ag}^{+}\right]^{3}\left[\mathrm{PO}_{4}^{3-}\right] \Rightarrow 1.8 \times 10^{-18}=(0.20+3 \mathrm{x})^{3}(\mathrm{x}) \approx(0.20)^{3}(\mathrm{x}) \\
& \mathrm{x}=2.2 \times 10^{-16} \mathrm{M} \mathrm{Ag}_{3} \mathrm{PO}_{4}
\end{aligned}
$$

Ion product, Q , is used to predict precipitation

1. $\mathrm{Q}>\mathrm{K} \quad$ supersaturated; precipitation occurs
2. $\mathrm{Q}<\mathrm{K} \quad$ unsaturated; can dissolve more!
3. $\mathrm{Q}=\mathrm{K} \quad$ saturated; precipitation and dissolution occur

## Precipitation Problems

Will barium hydroxide precipitate in a solution that is 0.20 M in sodium hydroxide and 0.10 M in barium nitrate? The $\mathrm{K}_{\mathrm{sp}}$ for barium hydroxide is $5.0 \times 10^{-3}$.
$\mathrm{NaOH} \Rightarrow 0.20 \mathrm{M} \mathrm{Na}^{+}$and $0.20 \mathrm{M} \mathrm{OH}^{-}$
$\mathrm{Ba}\left(\mathrm{NO}_{3}\right)_{2} \Rightarrow 0.10 \mathrm{M} \mathrm{Ba}^{2+}$ and $0.20 \mathrm{M} \mathrm{NO}_{3}{ }^{-}$
$\mathrm{Ba}(\mathrm{OH})_{2}(\mathrm{~s}) \rightleftharpoons \mathrm{Ba}^{2+}(\mathrm{aq})+2 \mathrm{OH}^{-}(\mathrm{aq})$
$\mathrm{K}_{\text {sp }}=\left[\mathrm{Ba}^{2+}\right]\left[\mathrm{OH}^{-}\right]^{2}=5.0 \times 10^{-3}$
$\mathrm{Q}=(0.10)(0.20)^{2}=4.0 \times 10^{-3}$
If $\mathrm{Q}<\mathrm{K}$, no precipitate forms

Will nickel (II) carbonate ( $\mathrm{K}_{\text {sp }}=1.4 \times 10^{-7}$ ) precipitate in a 1.00 L solution of 0.010 M nickel (II) nitrate and 0.025 M sodium carbonate?
$\mathrm{Ni}\left(\mathrm{NO}_{3}\right)_{2} \Rightarrow 0.010 \mathrm{M} \mathrm{Ni}^{2+}$ and $0.020 \mathrm{M} \mathrm{NO}_{3}^{-}$
$\mathrm{Na}_{2} \mathrm{CO}_{3} \Rightarrow 0.050 \mathrm{M} \mathrm{Na}^{+}$and $0.025 \mathrm{M} \mathrm{CO}_{3}{ }^{2-}$

$$
\begin{aligned}
& \mathrm{NiCO}_{3}(\mathrm{~s}) \rightleftharpoons \mathrm{Ni}^{2+}(\mathrm{aq})+\mathrm{CO}_{3}^{2-}(\mathrm{aq}) \\
& \mathrm{K}_{\mathrm{sp}}=\left[\mathrm{Ni}^{2+}\right]\left[\mathrm{CO}_{3}^{2-}\right]=1.4 \times 10^{-7} \\
& \mathrm{Q}=(0.010)(0.025)=2.5 \times 10^{-4}
\end{aligned}
$$

If $\mathrm{Q}>\mathrm{K}$, precipitate forms

What is the concentration of $\mathrm{Ni}^{2+}$ at equilibrium?
$\mathrm{Ni}^{2+}$ reacts with $\mathrm{CO}_{3}{ }^{2-} .$.

|  | $\mathrm{Ni}^{2+}(\mathrm{aq})+\mathrm{CO}_{3}{ }^{2-}(\mathrm{aq})$ | $\rightarrow$ | $\mathrm{NiCO}_{3}(\mathrm{~s})$ |
| :---: | :---: | :---: | :---: | :---: |
| I | 0.010 | 0.025 | $" 0 "$ |
| F | 0 | 0.015 | $" 0.010 "$ |

What is the concentration of $\mathrm{Ni}^{2+}$ at equilibrium?
Remaining $\mathrm{CO}_{3}{ }^{2-}$ acts as common ion...

$$
\begin{aligned}
& \mathrm{NiCO}_{3}(\mathrm{~s}) \rightleftharpoons \mathrm{Ni}^{2+}(\mathrm{aq})+\mathrm{CO}_{3}{ }^{2-}(\mathrm{aq}) \\
& \begin{array}{lll}
\mathrm{I} & 0 & 0.015
\end{array} \\
& \text { E } \quad x \quad x+0.015 \\
& \mathrm{~K}_{\mathrm{sp}}=\left[\mathrm{Ni}^{2+}\right]\left[\mathrm{CO}_{3}^{2-}\right] \Rightarrow 1.4 \times 10^{-7}=(x)(\mathrm{x}+0.015) \approx(\mathrm{x})(0.015) \\
& {\left[\mathrm{Ni}^{2+}\right]=\mathrm{x}=9.3 \times 10^{-6} \mathrm{M}}
\end{aligned}
$$

## Lewis Acids and Bases

Lewis acids are electron pair acceptors

Lewis bases are electron pair donors

Empty orbital of acid accepts electron pair from base in acid-base reactions


## Complex Ion Equilibria

Complex ions are formed from reactions of metal (atoms) ions and ligands

Ligands are molecules (ions) that donate electron pairs (Lewis bases!)

$$
\mathrm{Ag}^{+}+2:\left(\mathrm{NH}_{3}\right) \rightarrow \mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}
$$

Ligands add to metal ions in individual steps, each step described by a formation constant, $\mathrm{K}_{\mathrm{f}}$

$$
\begin{aligned}
& \mathrm{Ag}^{+}+\mathrm{NH}_{3} \rightleftharpoons \mathrm{Ag}\left(\mathrm{NH}_{3}\right)^{+} \mathrm{K}_{\mathrm{f} 1}=2.1 \times 10^{3} \\
& \mathrm{Ag}\left(\mathrm{NH}_{3}\right)^{+}+\mathrm{NH}_{3} \rightleftharpoons \mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}^{+} \\
& \hline \mathrm{K}_{\mathrm{f} 2}=8.2 \times 10^{3} \\
& \mathrm{Ag}^{+}+2 \mathrm{NH}_{3} \rightleftharpoons \mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}^{+}
\end{aligned} \mathrm{K}_{\mathrm{f}}=\mathrm{K}_{\mathrm{f} 1} \times \mathrm{K}_{\mathrm{f} 2}=1.7 \times 10^{7}
$$

What are the concentrations of all species in a solution that is initially $1.0 \times 10^{-3} \mathrm{M} \mathrm{Ag}^{+}$and $1.0 \mathrm{M} \mathrm{NH}_{3}$ ?

$$
\begin{aligned}
& \mathrm{Ag}^{+}+2 \mathrm{NH}_{3} \rightarrow \mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+} \quad \mathrm{K}_{\mathrm{f}}=1.7 \times 10^{7} \\
& \begin{array}{llll}
\text { I } & 0.0010 & 1.0 & 0
\end{array} \\
& \begin{array}{llll}
\text { F } & 0 & 0.998 & 0.0010
\end{array} \\
& \mathrm{Ag}^{+}+2 \mathrm{NH}_{3} \rightleftharpoons \mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+} \\
& \begin{array}{llll}
\text { I } & 0 & 0.998 & 0.0010
\end{array} \\
& \text { E } \quad \text { x } 0 . \underline{9} 98+2 x \quad 0.0010-x \\
& 1.7 \times 10^{7}=\frac{(0.0010-x)}{(x)(0.998+2 x)^{2}} \approx \frac{0.0010}{(x)(0.998)^{2}} \Rightarrow x=6 \times 10^{-11} \mathrm{M}
\end{aligned}
$$

What are the concentrations of all species in a solution that is initially $1.0 \times 10^{-3} \mathrm{M} \mathrm{Ag}^{+}$and $1.0 \mathrm{M} \mathrm{NH}_{3}$ ?

$$
\begin{aligned}
& {\left[\mathrm{Ag}^{+}\right]=\mathrm{x}=6 \times 10^{-11} \mathrm{M}} \\
& {\left[\mathrm{NH}_{3}\right]=0.998+2 \mathrm{x}=\underline{1 \mathrm{M}}} \\
& {\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}^{+}\right]=0.0010-\mathrm{x}=\underline{0.0010 \mathrm{M}}} \\
& \mathrm{Ag}\left(\mathrm{NH}_{3}\right)^{+}+\mathrm{NH}_{3} \rightleftharpoons \mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}^{+} \\
& \mathrm{K}_{\mathrm{f} 2}=\frac{\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}^{+}\right]}{\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)^{+}\right]\left[\mathrm{NH}_{3}\right]} \Rightarrow\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)^{+}\right]=\frac{\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}^{+}\right]}{\mathrm{K}_{\mathrm{f} 2}\left[\mathrm{NH}_{3}\right]} \\
& {\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)^{+}\right]=\frac{(0.0010)}{\left(8.2 \times 10^{3}\right)(1)}=\underline{1 \times 10^{-7} \mathrm{M}}}
\end{aligned}
$$

$\mathrm{K}_{\mathrm{f}}$ values can be used to predict stability of complex ions, sometimes called stability constants

Which is more stable?

$$
\begin{array}{ll} 
& \mathrm{Hg}(\mathrm{Cl})_{4}{ }^{2-}\left(\mathrm{K}_{\mathrm{f}}=1.2 \times 10^{15}\right) \\
\mathrm{Hg}(\mathrm{CN})_{4}{ }^{2-}\left(\mathrm{K}_{\mathrm{f}}=3 \times 10^{41}\right) \quad \text { Much more stable! } \\
\mathrm{Hg}(\mathrm{Cl})_{4}{ }^{2-} \rightleftharpoons \mathrm{Hg}^{2+}+4 \mathrm{Cl}^{-} & \mathrm{K}=\left(\mathrm{K}_{\mathrm{f}, \mathrm{Cl}}\right)^{-1} \\
\frac{\mathrm{Hg}^{2+}+4 \mathrm{CN}^{-}}{} \rightleftharpoons \mathrm{Hg}(\mathrm{CN})_{4}{ }^{2-} & \mathrm{K}=\mathrm{K}_{\mathrm{f}, \mathrm{CN}} \\
\mathrm{Hg}(\mathrm{Cl})_{4}{ }^{2-}+4 \mathrm{CN}^{-} \rightleftharpoons \mathrm{Hg}(\mathrm{CN})_{4}{ }^{2-}+4 \mathrm{Cl} & \mathrm{~K}=\left(\mathrm{K}_{\mathrm{f}, \mathrm{Cl}}\right)^{-1} \times \mathrm{K}_{\mathrm{f}, \mathrm{CN}}=2 \times 10^{26} \\
\text { Large } \mathrm{K}, \mathrm{Hg}(\mathrm{CN})_{4}{ }^{2-} \text { will be formed! } &
\end{array}
$$

## Solubility - An Equilibrium Position

The solubility of a salt is an equilibrium position
For a given temperature...
a single value for the solubility product constant ( $\mathrm{K}_{\mathrm{sp}}$ ) an infinite number of possible solubilities!

Solubility can be affected by:

1. the common ion effect
2. complex ion formation
3. changes in pH

## Complex Ions and Solubility

A number of insoluble salts can be dissolved upon formation of a complex ion...

AgCl

$$
\mathrm{K}_{\mathrm{sp}}=1.8 \times 10^{-10}
$$

$\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+} \quad \mathrm{K}_{\mathrm{f}}=1.7 \times 10^{7}$

$$
\begin{array}{rll}
\mathrm{AgCl} & \rightleftharpoons \mathrm{Ag}^{+}+\mathrm{Cl}^{-} & \mathrm{K}_{\text {sp }}=1.8 \times 10^{-10} \\
\mathrm{Ag}^{+}+2 \mathrm{NH}_{3} & \rightleftharpoons \mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}^{+} & \mathrm{K}_{\mathrm{f}}=1.7 \times 10^{7}
\end{array}
$$

$\mathrm{AgCl}+2 \mathrm{NH}_{3} \rightleftharpoons \mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}+\mathrm{Cl}^{-} \quad \mathrm{K}^{\prime}=\mathrm{K}_{\mathrm{f}} \times \mathrm{K}_{\mathrm{sp}}=3.1 \times 10^{-3}$

How much greater? $3.1 \times 10^{-3} / 1.8 \times 10^{-10}=17,000,000$ times!

## pH and Solubility

The solubility of a salt containing basic anion increases with increasing acidity

Basic anions are c. bases of weak acids:

$$
\mathrm{OH}^{-}, \mathrm{S}^{2-}, \mathrm{CO}_{3}^{2-}, \mathrm{PO}_{4}^{3-}, \mathrm{C}_{2} \mathrm{O}_{4}{ }^{2-}, \text { and } \mathrm{CrO}_{4}{ }^{2-}
$$

Basic anions react with hydrogen ions to form weak acid

$$
\begin{aligned}
\mathrm{Mg}(\mathrm{OH})_{2}(\mathrm{~s})+2 \mathrm{H}^{+}(\mathrm{aq}) & \rightleftharpoons \mathrm{Mg}^{2+}(\mathrm{aq})+2 \mathrm{H}_{2} \mathrm{O}(\mathrm{I}) \\
\mathrm{Ba}_{3}\left(\mathrm{PO}_{4}\right)_{2}(\mathrm{~s})+6 \mathrm{H}^{+}(\mathrm{aq}) & \rightleftharpoons 3 \mathrm{Ba}^{2+}(\mathrm{aq})+2 \mathrm{H}_{3} \mathrm{PO}_{4}(\mathrm{aq})
\end{aligned}
$$

If K is large, salt will be soluble under acidic conditions!

How much more?

$$
\begin{aligned}
\mathrm{Mg}(\mathrm{OH})_{2}(\mathrm{~s}) & \rightleftharpoons \mathrm{Mg}^{2+}(\mathrm{aq})+2 \mathrm{OH}^{-}(\mathrm{aq}) & \mathrm{K}_{\mathrm{sp}}=2.1 \times 10^{-13} \\
2 \mathrm{H}^{+}(\mathrm{aq})+2 \mathrm{OH}^{-}(\mathrm{aq}) & \rightleftharpoons 2 \mathrm{H}_{2} \mathrm{O}(\mathrm{l}) & 1 / \mathrm{K}_{\mathrm{w}}^{2}=1.0 \times 10^{28}
\end{aligned}
$$

$\mathrm{Mg}(\mathrm{OH})_{2}(\mathrm{~s})+2 \mathrm{H}^{+}(\mathrm{aq}) \rightleftharpoons \mathrm{Mg}^{2+}(\mathrm{aq})+2 \mathrm{H}_{2} \mathrm{O}(\mathrm{I})$

$$
\mathrm{K}^{\prime \prime}=\mathrm{K}_{\mathrm{sp}} / \mathrm{K}_{\mathrm{w}}^{2}=2.1 \times 10^{15} \ldots \text { or } 1.0 \times 10^{28} \text { times greater! }
$$

Again, you say?

$$
\begin{aligned}
\mathrm{Ba}_{3}\left(\mathrm{PO}_{4}\right)_{2}(\mathrm{~s}) & \rightleftharpoons 3 \mathrm{Ba}^{2+}(\mathrm{aq})+2 \mathrm{PO}_{4}^{3-}(\mathrm{aq}) \\
\begin{array}{ll}
6 \mathrm{H}^{+}(\mathrm{aq})+2 \mathrm{PO}_{4}^{3-}(\mathrm{aq}) & \rightleftharpoons 2 \mathrm{H}_{3} \mathrm{PO}_{4}(\mathrm{aq})
\end{array} & \begin{array}{l}
\mathrm{K}_{\mathrm{sp}}=6 \times 10^{-39} \\
\left(1 / \mathrm{K}_{\mathrm{a} 1} \mathrm{~K}_{\mathrm{a} 2} \mathrm{~K}_{\mathrm{a} 3}\right)^{2}
\end{array} \\
\mathrm{Ba}_{3}\left(\mathrm{PO}_{4}\right)_{2}(\mathrm{~s})+6 \mathrm{H}^{+}(\mathrm{aq}) & \rightleftharpoons 3 \mathrm{Ba}^{2+}(\mathrm{aq})+2 \mathrm{H}_{3} \mathrm{PO}_{4}(\mathrm{aq})
\end{aligned} \quad \begin{aligned}
\mathrm{K}^{\prime \prime}=\mathrm{K}_{\mathrm{sp}} /\left(\mathrm{K}_{\mathrm{a} 1} \mathrm{~K}_{\mathrm{a} 2} \mathrm{~K}_{\mathrm{a} 3}\right)^{2}=6 \times 10^{-39} /\left[\left(7.5 \times 10^{-3}\right)\left(6.2 \times 10^{-8}\right)\left(4.2 \times 10^{-13}\right)\right]^{2} \\
=1.6 \times 10^{5} \ldots \text { or } \sim 3 \times 10^{43} \text { times greater! }
\end{aligned}
$$

